

Star Formation Thresholds in Galactic Disks¹

Crystal L. Martin

Astronomy Department, California Institute of Technology, MC 105-24, Pasadena, CA
91125

and

Robert C. Kennicutt, Jr.

Steward Observatory, University of Arizona, Tucson, AZ 85721

ABSTRACT

We report the first results of a detailed study of the star formation law in a sample of 32 nearby spiral galaxies with well-measured rotation curves, HI and H₂ (as traced by CO) surface density profiles, and new H α CCD photometry. In this paper we present an atlas of H α images and radial surface brightness profiles and describe a surface-density threshold in the star formation law. Prominent breaks in the H α surface-brightness profiles are identified in nearly all of the actively star-forming disks, confirming previous claims of star formation thresholds based on lower quality data. We measure the ratio of the gas density to the critical density for local gravitational stability at the threshold radii. The outer threshold radii observed in Sab–Sdm galaxies are in general agreement with those expected from the Toomre Q stability criterion, confirming earlier work, but with a significant variation that appears to be weakly correlated with galaxy type. Such a trend could plausibly reflect variations in the relative contribution of the stellar disk to the instability of the gas disk across this range of galaxy types. Among disks with sub-critical gas surface densities, and outside the threshold radius in star-forming disks, the number of isolated HII regions increases as the gas surface density approaches the critical density. At the thresholds, the gas surface densities span a wide range; and the atomic/molecular gas fraction is highest in the disks having the lowest total gas surface density. The simple Toomre condition fails to account for the active star formation in the inner disks of low-mass spirals such as NGC 2403 and M33. An alternative stability criterion based on the shear

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in the disk provides a better description of these disks but is a less accurate indicator of the outer edges of star-forming disks than the Toomre criterion. These results strongly support the view that the formation of gravitationally bound interstellar clouds regulates the onset of widespread star formation – at least in the outer regions of galactic disks.

Subject headings: galaxies: ISM – galaxies: evolution – stars: formation – galaxies: stellar content

1. Introduction

The evolution of galaxies is strongly influenced by how quickly gas is consumed by stars. Most simulations assume the star formation rate (SFR) scales as a power law of the gas density as originally proposed by Schmidt (1959) or adopt the surface density parameterization introduced by Kennicutt (1989). A global correlation between SFR and gas surface density ($\Sigma_{SFR} \propto \mu_{gas}^{1.4}$) is obtained empirically when both quantities are normalized by the area of the stellar disk. Since galaxies typically have gaseous disks that are significantly larger than their stellar disks (e.g. Warmels 1988a; Warmels 1988b; Gallagher & Hunter 1984), the gas in the outer disk is not included in the surface density measurement (Kennicutt 1998). The empirical star formation recipe implicitly includes a surface density threshold for star formation, and this should be incorporated in the prescriptions used in numerical simulations.

The idea that gravitational instability might determine the critical gas density for star formation was introduced by Spitzer (1968) and Quirk (1972) soon after local stability criteria for differentially rotating disks were developed (Toomre 1964; Goldreich & Lynden-Bell 1965). A thin, gas disk is unstable to axisymmetric disturbances where the Toomre Q parameter,

$$Q(R) \equiv \frac{\sigma \kappa}{\pi G \mu}, \quad (1)$$

is less than unity. The epicyclic frequency, κ , velocity dispersion, σ , and surface density, μ , refer to the gas disk at galactocentric radius R . Widespread star formation is expected where the gas surface density exceeds the critical surface density defined as

$$\mu_{crit} = \alpha_Q \frac{\sigma \kappa}{\pi G}, \quad (2)$$

The parameter α_Q is fitted to the threshold values of the radially varying quantity

$$\alpha(R) = \mu_{gas}(R) / \mu_{crit}(R) \quad (3)$$

and makes allowances for deviations from the idealized thin disk model such as finite scaleheight or the presence of a stellar disk. The velocity dispersion is predicted to remain roughly constant in self-regulated regions of disks (Silk 1997) and may have a lower bound set by the dissipation of MHD-driven turbulence in the outer disk (Sellwood & Balbus 1999). If the gas velocity dispersion does not vary much with radius across a spiral galaxy, then the critical surface density falls as roughly R^{-1} . This gradient is shallower than the decline in the total gas surface density with radius, so the critical density will exceed the gas surface density at some threshold radius. Gravitational stability therefore provides an appealing explanation for the rather sharp edges of stellar disks (van der Kruit & Searle 1981a,b; 1982a,b).

Kennicutt (1989) directly tested this hypothesis using the radial distribution of HII regions to trace the SFR. He adopted a constant gas velocity dispersion of 6 km s^{-1} and found the Schmidt law broke down at radii where the gas surface density was less than $0.63\mu_{crit}$ (Kennicutt 1989²). The gas surface density in low surface brightness galaxies was subsequently shown to be below the critical density for gravitational instability, and gravitational thresholds were used to explain the low level of star formation activity in these gas-rich galaxies (van der Hulst et al. 1993; van Zee et al. 1997; van Zee et al. 1996). More recently, Ferguson et al. (1998) have questioned the validity of a constant gas velocity dispersion. Since measurements of the HI velocity dispersion demand both high angular resolution and high brightness sensitivity – requirements not met by most observations, the most feasible way forward currently is a comparison of measured threshold radii to the thresholds predicted using constant velocity dispersion in a large sample of galaxies.

Hunter et al. (1998) have recently questioned the utility of the Toomre criterion for describing star-formation thresholds. They measure a mean value of α_Q in irregular galaxies that is a factor of two lower than that found by K89 for spiral galaxies. This result implies that the gas in the irregular galaxies is less stable than the gas in spiral galaxies. In addition to the absence of spiral density waves in irregular galaxies, these disks have less rotational shear on average. (i.e. Their rotation curves are closer to solid body.) If the local shear rate, rather than the Coriolis force (essentially κ), best describes the destruction rate of giant clouds, then the stability criterion would need to be modified (Elmegreen 1987; Elmegreen 1993; Elmegreen 1991). For example, the local shear rate is described by the Oort A constant,

$$A = -0.5R \frac{d\Omega}{dR}. \quad (4)$$

Following Elmegreen (1993) and Hunter, Elmegreen, & Baker (1998, hereafter HEB98)

²K89 reported a value of $\alpha_Q = 0.67$ but used a constant of 3.36 rather than π in eq. (1).

shearing perturbations grow at the rate $\pi G\mu/\sigma$, and the critical column density for significant growth in the presence of shear becomes

$$\mu_{crit}^A \approx \frac{\alpha_A A \sigma}{\pi G}, \quad (5)$$

and $\alpha_A \approx 2.5$. This surface density threshold is extremely low in the inner regions of galaxies with slowly rising rotation curves but approaches the Toomre stability condition where the rotation speed is constant.

In addition to this degeneracy, many other descriptions of star formation thresholds including gas deficiencies in the outer disk (Warmels 1988a; Cayatte et al. 1990), the phase structure of the interstellar gas (Elmegreen & Parravano 1994), or the radiative feedback from young stars have been advanced (Federman et al. 1979; Skillman 1987). With such a broad array of physical processes at work, the K89 analysis should be repeated on a larger, more diverse sample of galaxies. The $H\alpha$ surface brightness profiles presented in this paper supercede those in the K89 paper which were based largely on HII region counts. The $H\alpha$ images presented alongside the threshold measurements should resolve the confusion which has arisen regarding what is meant by a threshold radius (Ferguson et al. 1998). Finally, the number of galaxies with published CO observations has greatly increased in the last decade, due in large part to the Five College Radio Astronomy Observatory (FCRAO) CO survey (Young et al. 1995). Hence, it is now possible to examine the full range of spiral galaxy types using atomic and molecular gas data compiled from the published literature.

The paper is organized as follows. In §2 we describe our $H\alpha$ observations and the atomic and molecular gas data used in our new analysis. In §3 we identify the star formation thresholds, measure gas densities at the thresholds, and evaluate the Toomre stability criterion. In §4, we discuss the failures of the model, the shear criterion for stability, the influence of the stellar disk on the stability criterion, and the implications for the global star formation rate. The data presented here will be used to discuss the processes regulating the SFR in the high density regime (i.e. where gas surface density exceeds the threshold density) in a subsequent paper.

2. Data

We selected 32 spiral galaxies divided roughly evenly between types Sab and Sdm that had published ^{12}CO ($J = 1 - 0$) and 21-cm radial intensity profiles. Nearly half the galaxies are Virgo Cluster members, and 15 of the galaxies are classified as barred galaxies in the RC1 (de Vaucoulers system). In the K89 paper, radial profiles were estimated for 16 galaxies from HII region counts. That subsample was dominated by type Sc galaxies.

Table 1 lists the type, distance, and disk inclination for each galaxy in our sample. The critical density of a disk scales inversely with the assumed distance and is the only distance-dependent quantity that enters our analysis. Most of the distances come from measurements of Cepheid variables. We correct surface brightness, surface density, and rotation speed measurements for disk inclination. Disk inclinations and position angle were generally adopted from 21-cm observations. If these values were heavily weighted by HI beyond the optical disk, we used the shape of the optical continuum isophotes to derive a disk inclination and position angle. The position angles are given in Table 1 and describe the major axis of elliptical apertures used in our $H\alpha$ photometry.

2.1. $H\alpha$ Imaging

We use recombination line radiation from hydrogen to trace the location of young, massive stars in the disks. The $H\alpha$ line was chosen for the imaging because only optical CCD cameras offered a wide enough field of view to cover the entire disk in one or two pointings per galaxy. The measured $H\alpha$ luminosities can be directly converted to SFR’s using the calibration of Kennicutt, Tamblyn, & Congdon (1994) –

$$\text{SFR}(\text{M}_{\odot} \text{ yr}^{-1}) = \frac{L_{H\alpha}}{1.25 \times 10^{41} \text{ ergs s}^{-1}} 10^{0.4A(H\alpha)}. \quad (6)$$

This relation was derived using a Salpeter initial mass function, $dN(m)/dm = m^{-2.35}$, for stellar masses between $m = 0.1$ and 100 M_{\odot} . The stars were evolved along the evolutionary tracks of Schaller et al. (1993), and the ionizing flux calculated from Kurucz (1992) model atmospheres. The amount of extinction at $H\alpha$, $A_{H\alpha} = 0.78A_V$ (Miller & Mathews 1972), is the largest source of uncertainty in the measured SFR.

Narrowband continuum and $H\alpha$ images were obtained at the Steward Observatory Bok telescope, KPNO Burrell-Schmidt telescope, and KPNO 36-in telescope. These CCD frames were corrected for fixed pattern noise in the standard way using a bias frame, dome flat, and sky flat. The 90-in data were obtained with a focal reducer, and scattered light produced ghost images which had to be removed in the background subtraction. Foreground stars were used to register the images and subtract the continuum emission from each narrowband $H\alpha$ image. The line flux was then corrected for atmospheric extinction and the transmission of the filter at $H\alpha$ relative to the average transmission over the bandpass. Data obtained at the Bok telescope and Burrell-Schmidt telescope were flux calibrated using observations of standard stars. The five galaxies observed at the Kitt Peak 36-in and NGC 7331, NGC 925, NGC 628, and NGC 4402 were calibrated from the integrated fluxes of Kennicutt & Kent (1983) or Kennicutt (1998). The Burrell-Schmidt images do not

include [NII] emission, so we increased their flux by a spectroscopically-determined factor ranging from 1.2 to 1.4 to consistently include [NII] emission. Figure 1 compares our $H\alpha$ + [NII] $\lambda\lambda 6548, 83$ fluxes to previously published work. The independent measurements are typically consistent to within 15%.

The radial distribution of $H\alpha$ emission was measured from surface photometry. The optical nucleus of each galaxy defines the center of a set of concentric, elliptical apertures. The width of the annuli is a tradeoff between the desire to average over individual HII regions and the need to accurately measure breaks in the profile. A width of about $10''$ proved to be a good compromise for most of the galaxies. The profiles changed very little if this width was changed by a factor of two. The profiles were corrected to face-on orientation.

To convert the surface brightness profiles in Figure 3 to SFR per unit area, we recommend applying an internal extinction correction, $A_{H\alpha} = 1.1$ mag, derived from comparison of the free-free radio emission and the $H\alpha$ emission from spiral galaxies (e.g. van der Hulst et al. 1988). Correction for [NII] emission in the bandpass reduces the SFR by 15% to 30%. Radial gradients in internal extinction are typically not strong compared to the scatter in extinction at a given radius (e.g. Zaritsky, Kennicutt, & Huchra 1994, Webster & Smith 1983, McCall et al. 1985). An exception is the nuclear region. The central star formation rates implied by these profiles are highly uncertain due to the unknown amount of dust obscuration, photoionization by an active nuclei, and continuum subtraction errors.

The limiting surface brightness was estimated from the uncertainty in the background and the area of the aperture and then verified by adding fake sources to the images. Where the covering factor of HII regions was low, photometry could be obtained for individual HII complexes using local background measurements. In other regions, variations in the mean background level dominate the uncertainty in the photometry. In particular, scattered light in the focal reducer camera at the Bok telescope produced ghost images that were easily identified by eye but difficult to model and subtract. We used a mean background measurement, and then estimated the maximum error using the full range of mean background levels on the frame. The errorbars shown on the radial profiles are therefore maxima and minima in these regions.

2.2. Molecular Gas Surface Densities

Only a few galaxies in the sample have been completely mapped in the ^{12}CO ($J = 1 - 0$) line. FCRAO maps have been published for NGC 5194 (Lord & Young 1990) and NGC 6946 (Tacconi & Young 1989). The galaxies NGC 5457 (Kenney et al. 1991), NGC 3031 (Sage & Westphal 1991), NGC 5236 (Crosthwaite & Turner in prep), and the inner 3.2 kpc of NGC 2403 (Thornley & Wilson 1995) have been mapped with the NRAO 12m telescope. For the rest of our sample, the CO radial profiles represent measurements made along the major axis of each galaxy. These profiles have a resolution of $\sim 45''$. The data are described in detail in survey papers by Kenney & Young (1988) and Young et al. (1995).

These source papers adopt CO-to- H_2 conversion factors based on Galactic calibrations. We follow this convention but adopt a common scale of

$$N(\text{H}_2) = (2.8 \times 10^{20} \text{ cm}^{-2}) I_{\text{CO}}(K(T_R) \text{ km s}^{-1}) \quad (7)$$

(Bloemen et al. 1986) for all the galaxies. The beam-averaged brightness temperature, T_R , inferred from the measured antenna temperature depends on the source-beam coupling efficiency and the forward scattering and spillover efficiency as described, for example, by Kenney & Young (1988) and Young et al. (1995). We adopted their calibrations, $\eta_{fss} = 0.75$ and $\eta_c = 0.73$, for the FCRAO survey data. The NGC 5194 profile uses $\eta_{fss} = 0.70$ and $\eta_c = 0.69 - 0.81$ following the model of Lord & Young (1990). The NRAO 12m source-beam coupling efficiency derived for M101 (Kenney et al. 1991) was applied to the M81 data. The H_2 gas surface density was multiplied by a factor $1.4 \cos(i)$ to correct for inclination and to include the He mass.

2.3. Atomic Gas Surface Densities

The HI radial profiles were taken from 21 cm observations listed in Table 1. The profiles from the Warmels (1998c) paper were derived from strip scans across each galaxy with the Westerbork Synthesis Radio Telescope. The half-power beam width was about $12''$ in right ascension by $12''(\sin(\delta))^{-1}$ in declination. These scans are essentially major axis profiles for many of the galaxies, but the scans are aligned closer to the minor axis of NGC 4178, NGC 4321, NGC 4501, NGC 4535, NGC 4548, and NGC 4689.

The other profiles were obtained by integrating over ellipses and correcting to face-on orientation. The typical half-power beam width of the other WRST maps is 30 - 60'' (Wevers 1984; Bosma 1981; Bosma 1977; Bosma et al. 1981; Rots 1975). The WSRT observations of NGC 5194 (Tilanus & Allen 1991) and NGC 5236 (Tilanus & Allen 1993) have higher

resolution. The surface density profile for NGC 6946 comes from a Very Large Array map (Tacconi & Young 1986) with $40''$ resolution. Braun et al. (1994) describe the compilation of WRST and VLA observations used to construct the high resolution HI map of NGC 4826.

2.4. Gas Kinematics

Rotation curves are needed to calculate radial stability profiles for each galaxy. Our analysis uses the HI 21-cm rotation curves derived by Wevers (1984) and Guhathakurta (1988) and position – velocity diagrams published by Warmels (1988a, 1988b). Velocities measured from CO observations were included in the rotation curves for NGC 5194, NGC 5457, and NGC 4321 (Kenney & Young 1988; Young et al. 1995; Sofue 1996). These CO and HI 21-cm observations lack sufficient spatial resolution to determine the kinematics in the inner $\sim 45''$ of the disks. Optical emission-line velocities were used to improve inner rotation curves of NGC 4548 and NGC 4639 (Rubin et al. 1999). In general, the dynamics of the inner disk are not well constrained by the observations compiled here, and our stability analysis will focus on the outer regions of disks.

Measurements of the HI velocity dispersion are difficult to make in galaxies that are inclined enough (relative to our sightline) to accurately model their rotation curves. Studies of spiral galaxies find $\sigma = 3 - 10 \text{ km s}^{-1}$ in the outer disk (van der Kruit & Shostak 1984; Dickey et al. 1990). A similar range is estimated for dwarf irregular galaxies – $7.6 - 11.4 \text{ km s}^{-1}$ (van Zee et al. 1997). The higher velocity dispersions tend to be associated with the regions of higher star formation activity (Shostak & van der Kruit 1984; Jogee 1999). We adopt $\sigma = 6 \text{ km s}^{-1}$ to facilitate comparison with K89.

3. Testing the Gravitational Stability Model at the Star Formation Thresholds

To give the reader an appreciation of the accuracy with which the stability criterion can be evaluated, we step through our analysis of NGC 5236. Our H α atlas is then used to further illustrate what is meant by the expression *star formation threshold*. We describe the properties of the gas disks at the thresholds and evaluate the local stability of the disks using the single-fluid model.

3.1. Case Study: NGC 5236

Figure 2 shows that the broken spiral pattern of $H\alpha$ emission from NGC 5236 creates a smooth radial surface brightness profile, which is well fitted by an exponential profile over a wide annulus. The strongest break in the radial profile defines the threshold radius, $R_{\text{HII}} = 305''$. The azimuthally-averaged SFR there is $0.0027 \text{ M}_{\odot} \text{ yr}^{-1} \text{ kpc}^{-2}$, but the best estimate for the upper limit just 500 pc further out is 100 times lower. The $H\alpha$ surface brightness is also low in the inner disk, where the star-forming regions are concentrated along the bar; but the magnitude of the deficit relative to the fit is much smaller. In Figure 3, a few HII regions are seen beyond R_{HII} , but their covering factor is much, much lower than in the region $R \leq R_{\text{HII}}$. The threshold radius derived from the azimuthally-averaged $H\alpha$ profile is a good approximation to the 'edge' of the star-forming disk, but it does overestimate the threshold radius at some position angles (e.g. northeast side of NGC 5236) since the shape of the $H\alpha$ isophotes changes slightly with galactocentric radius.

The middle panel of Figure 2 compares the radial variation in the azimuthally-averaged HI surface density (Tilanus & Allen 1993, TA93) to the variation in molecular gas surface density along the major axis (Young et al. 1995). More recent CO mapping across NGC 5236 (Crosthwaite & Turner, private communication) shows the molecular gas is concentrated along the bar near the major axis. We find the spatial mismatch (one-dimensional cut vs. azimuthal averaging) exaggerates the central depletion of atomic gas relative to molecular gas. The azimuthal gas distribution is more uniform further out in this disk. For many galaxies in our sample, complete two-dimensional mapping of the gas distribution is not available. This example draws attention to the systematic errors introduced by using the one-dimensional cuts and suggests they are significant in the inner disk when a gaseous bar is present. They do not affect the measurement of the total gas density at the threshold radius in NGC 5236. When the $H\alpha$ surface brightness is plotted against the total gas density, a strong break is seen at the outer threshold. This $\log \Sigma$ vs. $\log \mu$ relation is well described by a power law over most of the disk, but the spatial mismatch between the atomic and molecular gas sampling in the inner disk artificially adds some structure to it.

The critical density for local gravitational instability, as defined by the Toomre Q criterion, is also shown in the middle panel of Figure 2. The gas velocity dispersion is assumed to be constant, so the small-scale features reflect structure in the rotation curve of TA93 through the epicyclic frequency,

$$\kappa^2(R) = 2\left(\frac{V^2}{R^2} + \frac{V}{R} \frac{dV}{dR}\right). \quad (8)$$

The rotation curves typically represent an average $V(R)$ fitted to the two-dimensional

velocity field or to both sides of the major axis. The ratio of the total gas density to the critical density, bottom panel of Figure 2, falls steadily with radius beyond the bar region. The spatial resolution of the rotation curve is insufficient to describe the critical density at radii less than $\sim 45''$. At the star-formation threshold R_{HII} , the gas density, $10 \text{ M}_{\odot} \text{ pc}^{-2}$, is 70% of the critical density for instability ($\alpha(R_{\text{HII}}) = 0.7$), as given in eq (2) for $\sigma = 6 \text{ km s}^{-1}$. In NGC 5236, the dominant error in $\alpha(R_{\text{HII}})$ is the extrapolated molecular gas density. If the molecular gas disk is truncated abruptly at $R \approx 250''$, then the value of $\alpha(R_{\text{HII}})$ could be as low as 0.25. This scenario is unlikely as it would produce a strong discontinuity in the total gas surface density. However, fitting the exponential profile to only the less sensitive data ($R_{\text{CO}} = 150''$ instead of $R_{\text{CO}} = 250''$) yields a flatter gradient in the molecular gas density and overestimates the threshold gas density by $\sim 40\%$. This type of systematic error appears to dominate the systematic error in $\alpha(R_{\text{HII}})$ for a number of galaxies in our sample.

3.2. Threshold Radii

Figure 3 shows $\text{H}\alpha + [\text{NII}]$ images and radial surface brightness profiles for the entire sample. The threshold radii are marked. Star formation thresholds, as described for NGC 5236, are easily identified in 27 of the 32 galaxies in the sample. In most of these galaxies the drop in SFR per unit area at the threshold is very sharp, declining by a factor of 3 to 400 over a single $10''$ resolution element. The change in star formation efficiency, i.e. SFR per unit gas mass, is similar. The profiles for NGC 2903, NGC 4535, and NGC 4736 do not show such strong discontinuities, but the sharp change in profile slope in the outer disks do seem to reflect some type of threshold in the star formation law. The $\text{H}\alpha$ surface brightness in NGC 2841 and NGC 4698 is too low to determine whether the threshold effect is present.

In many disks, HII regions are seen beyond the threshold radius (Ferguson et al. 1998; Lelievre & Roy 2000). Their covering factor is much lower than it is within the main star-forming disk ($R < R_{\text{HII}}$). It seems plausible that the local $\mu_{\text{gas}} / \mu_{\text{crit}}$ ratio is higher in these regions. In NGC 2903 for example, the HII regions beyond the threshold radius are clearly associated with density perturbations caused by the spiral arms. The closer the mean gas density is to the critical density, the more frequently we expect a given region to experience a perturbation sufficient to bring it above the threshold.

3.3. Sub-Critical Disks

Our sample contains seven sub-critical disks where α never reaches the empirically-defined threshold value – $\alpha_Q = 0.63$ in K89 and $\alpha_Q = 0.69$ in a subsequent section of this paper. One member of our sample with a sub-critical disk, NGC 2403, shows widespread star formation activity, and this failure of the Toomre-criterion will be discussed later. Figure 4 shows the instability profiles for the other six galaxies with sub-critical disks. The gas density becomes a progressively larger fraction of the critical density (at the radius of maximum α (R)) in this order – NGC 4698, NGC 4639, NGC 3031, NGC 2841, NGC 4548, NGC 4571.

To facilitate comparison of their HII region distributions, the six galaxies are displayed with the same intensity limits in Figure 3. Starting with the most stable disk in the sample, NGC 4698, only a few, small HII regions are detected. The HII regions in NGC 3031 are confined to the spiral arms whose extent may be set by an outer Linblad Resonance (cf. Adler & Westpfahl 1996, but also Westpfahl 1998). The distribution of HII regions is much more widespread in NGC 2841 consistent with an instability that approaches the critical value. In NGC 4548, the annulus extending from about $0.5 R_{\text{HII}}$ to R_{HII} is near the instability limit, and a pair of spiral arms is present there. The bar in NGC 4548 and ram pressure stripping have strongly influenced the gas distribution (Vollmer et al. 1999) and consequently the star formation. This comparison indicates that – (1) external perturbations have an important impact on where star formation occurs in sub-critical disks, and (2) HII regions become more prevalent as the instability parameter increases.

The paucity of star formation in these six galaxies cannot be attributed to low gas surface density. The disk of NGC 4698 is a special case in as much as the gas was probably removed in a collision with another galaxy (Valluri et al. 1990). The gas surface density in 3 of the other 5 sub-critical disks exceeds the median threshold density (see next section). This result has implications beyond early-type spiral galaxies. Low surface brightness galaxies also present a sparse distribution of HII regions and sub-critical gas densities (van der Hulst et al. 1993), but the paucity of HII regions can be attributed to the low gas surface density (only a few solar masses per square parsec). Our analysis strongly suggests that it is the ratio $\frac{\mu_{\text{gas}}}{\mu_{\text{crit}}}$ rather than the gas surface density alone that sets the threshold for widespread star formation.

3.4. The Relative Fraction of Atomic and Molecular Gas

Using the data described in § 2, we measured the surface density of atomic and molecular gas at R_{HII} in each galaxy. Figure 6 shows the gas surface density ranges from 0.7 to 40 $M_{\odot} \text{ pc}^{-2}$ at the outer threshold. In a few galaxies with prominent gas rings, like NGC 4402 and NGC 5055, the apparent edge of the molecular gas disk does appear to be associated with the edge of the star-forming disk. However, in half of the galaxies in our sample, atomic gas contributes most of the gas surface density at R_{HII} . In eight galaxies, the molecular gas surface density is essentially zero at R_{HII} for any reasonable extrapolation of the CO intensity profile, and threshold radii predicted from the molecular gas density alone would grossly underestimate the observed threshold radii. (The individual star-forming regions almost certainly contain unresolved molecular clouds, but their contribution to the gas surface density is apparently negligible in these regions.) Any viable threshold mechanism must explain the wide range in $\mu_{\text{gas}}(R_{\text{HII}})$ and not depend on whether the gas is in atomic or molecular form. The gravitational stability model meets both of these criteria. We emphasize that it predicts the formation of large, self-gravitating clouds not stars. The good agreement with the observed radii of the star-forming disks, however, strongly suggests that star formation will happen once the clouds form.

At the median threshold gas density the atomic gas fraction ranges from 20% to 100%. Yet at densities twice as high, the ISM is almost entirely molecular. The gas is almost entirely atomic at surface densities that are half the mean. Much of the gas mass is in molecular form in disks with high gas surface densities, including the sub-critical disk of NGC 2841. The high atomic gas fractions in the other sub-critical disks are consistent with their average to low gas density. This division in atomic gas fraction is expected if the column of HI required to shield the molecular gas from radiation (that would dissociate it) is fairly uniform among disk galaxies. The implied threshold column for molecular gas formation ranges from 5 to 15 $M_{\odot} \text{ pc}^{-2}$.

It is interesting to examine whether the disks that are mostly molecular at R_{HII} become dominated by HI where the gas surface density drops into the 5 to 15 $M_{\odot} \text{ pc}^{-2}$ range. Generally, we find that no CO emission is detected at this radius, so the data for the outer disks are consistent with the same H_2/HI self-shielding column density. The only disk that clearly has a low atomic gas fraction at low total gas column is NGC 4579.

3.5. The Instability Parameter at the Outer Threshold

Critical surface densities for instability were computed from the rotation curves and compared to the gas densities described in the previous section. The median value of the instability parameter at the outer thresholds, $\alpha_Q = 0.69$, was found to be consistent with the K89 value. To reveal the physical limitations of this model, we examine the stability of the disks at the threshold radii in greater detail than previous work. Three types of second order effects are examined: (1) Does the scatter in the α (R_{HII}) values reflect the accuracy of the model or the magnitude of systematic errors?, (2) Can the sharpness of the threshold be predicted from the stability properties of the disk?, and (3) Is the stability of the gas disk influenced by the stellar disk?

3.5.1. Disk Asymmetry

The epicyclic frequency and, consequently, the critical density have significant errors where the rotation curve is poorly determined as in highly inclined disks, disks with kinematic disturbances near R_{HII} , and disks with offset dynamical and photometric centers. Within our sample, the projection effects are largest for NGC 628 where a 1° uncertainty in the disk inclination implies a 20% uncertainty in μ_{crit} . The rotation curves of NGC 5457 and NGC 5194 are not well defined at R_{HII} due to tidal disturbances, so the threshold instability parameter is not defined in these two galaxies. The dynamical center of NGC 925 is not coincident with the photometric center (in $\text{H}\alpha$, continuum, or HI) – a situation common in barred Magellanic irregulars (Pisano et al. 2000 and references therein). In general though, uncertainty about μ_{crit} is small compared to the error in the μ_{gas} measurement.

The largest systematic errors in the measurement of μ_{gas} are introduced by the asymmetry of the star-forming disks – i.e. the lack of axial symmetry or roundness. To quantify the impact on the threshold measurements, we measured a threshold radius and stability profile along the major axis of each galaxy. Comparison to the azimuthally-averaged quantities reveals the magnitude of the azimuthal variations in the instability parameter. The largest variations are illustrated in Figure 7. We find the following correlations between the instability parameter and the distribution of star formation in these disks.

1. Recent star formation activity in NGC 4254 is skewed toward the north-eastern half of the disk. The threshold radius on the western side is only 60% of its average value. The instability parameter along the eastern side of the major axis is also higher than it is on the western side. The threshold radius and stability parameter derived from

the azimuthally averaged profile are heavily weighted by the eastern side of the disk.

2. In NGC 4321, the average threshold radius R_{HII} provides a poor description of the irregular outer, $\text{H}\alpha$ isophotes. At a position angle of 90° for example, the HII regions extend to a radius of $0.9R_{\text{HII}}$ to the west but only $0.6R_{\text{HII}}$ to the east. Inspection of Figure 3 shows the two-arm spiral pattern also loses its definition at these radii. The surface density is $\sim 0.7\mu_{\text{crit}}$ at the threshold along either direction of this cut because the gas density declines much more steeply with radius on the east side of the galaxy. In contrast, when the gas densities from each side of this disk are averaged together, the value of the instability parameter at R_{HII} is underestimated by a factor of two! Better spatial coverage drives the threshold stability parameter toward $\alpha(R_{\text{HII}}) = 0.7$.
3. The star formation activity in NGC 4654 extends furthest to the south-east, but the HII regions are faint and sparse here. The $\text{H}\alpha$ surface brightness is much higher on the western side of NGC 4654 where the star formation threshold is much sharper. The gas surface density is sub-critical over much of the eastern side of the galaxy and super-critical on the western side – consistent with the paucity of HII regions to the east. On the eastern side, the instability parameter decreases more slowly with radius, however, explaining the larger radial extent of the HII regions. The sharp gradient in the instability parameter on the western side is likely not resolved, so the value of the instability parameter, $\alpha = 1.6$, at the western threshold is overestimated.
4. In NGC 7331, the star formation activity is skewed toward the southern half of the disk. The azimuthally-averaged $\text{H}\alpha$ profile is weighted toward this side of the disk, so the southern edge of the star-forming disk defines R_{HII} . Along the southern side of the major axis, the gas density is $0.8\mu_{\text{crit}}$ at R_{HII} . At this radius, $\alpha = 0.4$ on the northern side of the disk. However, at the smaller radius defined by the northern edge to the star-forming disk, the gas density is $0.6\mu_{\text{crit}}$. In this case the azimuthally-averaged value of the instability parameter, $\alpha(R_{\text{HII}}) = 0.4$, clearly underestimates the true value at the edge of the star-forming disk.

We have demonstrated that using azimuthally-averaged gas densities and SFR's can lead to errors in $\alpha(R_{\text{HII}})$ as large as a factor of two when the disk is highly non-axisymmetric. The theoretical basis for the Toomre stability criterion breaks down in these irregular systems, so it is noteworthy that a local Q criterion appears to be so useful in describing the distribution of star formation in these highly disturbed disks. The examples presented demonstrate that the distribution of star-forming regions clearly becomes much more sparse, similar to the subcritical disks, in regions where the instability parameter is low. The threshold values of the instability parameter also show a tendency to converge when better spatial coverage is used.

3.5.2. Star Formation Beyond the Threshold Radius

Gravitational threshold models only predict a sharp edge to the star-forming disk if the gas disk is perfectly smooth. The structure of the interstellar medium in real galaxies must modify this picture (Kennicutt 1989). Non-axisymmetric modes and local perturbations generate structure on large and small scales, respectively. Such regions may allow cloud formation (and subsequently star formation) even where the azimuthally-averaged gas density is sub-critical. For example, in § 3.3, the spiral density waves in the subcritical disks of NGC 3031 and NGC 4548 are supported where the gas surface density exceeds $0.3\mu_{crit}$ rather than $0.69\mu_{crit}$. The lower threshold is consistent with models of swing amplification. The more isolated HII regions in the subcritical disks are generated by a different mechanism. We suggest that random density perturbations generate some super-critical regions in disks that have surface densities close to the critical density for instability. Support for this viewpoint comes from the sub-critical disks. Isolated HII regions were found most frequently when the gas surface density was only slightly sub-critical, and no HII regions were found where the gas surface density was less than 10% of the critical density. As the average gas surface density approaches the critical density, the amount of star formation activity in isolated, star-forming regions clearly increases. Could a combination of local perturbations and spiral arms also explain the existence of HII regions at radii beyond the threshold radius? If so, star formation activity should be more prevalent where the μ_{gas} / μ_{crit} ratio remains high (i.e. greater than 0.3) beyond R_{HII} .

To test this hypothesis, we need to minimize the systematic errors caused by disk asymmetry at R_{HII} , so we compare the 11 galaxies with the smallest azimuthal variations in threshold radius. Figure 8 shows the radial stability profiles for ten members of our sample; the profile for NGC 5236 was shown previously. The spread in the instability parameter is only a factor of two at the threshold radius where the profiles converge. Beyond the threshold radius, the shallowest gradient is found in the disk of NGC 2403 which remains marginally stable. Not surprisingly, many HII regions are seen beyond R_{HII} in NGC 2403. The gas surface density in NGC 6946 also remains close to the critical density, i.e. $\mu_{gas} \geq 0.4\mu_{crit}$, out to $2R_{HII}$; and a large number of HII regions are seen beyond R_{HII} (cf. Ferguson et al. 1998). In contrast, the steepest gradients in the instability parameter,

$$\left| \frac{d(\mu_{gas}/\mu_{crit})}{dR} \right| > 0.1 \text{ kpc}^{-1}, \quad (9)$$

are found in NGC 4402, NGC 4713, and NGC 5236. None of these galaxies show much H α emission beyond the threshold radius. The instability parameter is also low outside the threshold radius in NGC 2903, but the star formation is confined to the spiral arms. locally. The likelihood of finding isolated HII regions outside R_{HII} therefore appears to scale with

the value of the instability parameter.

It is interesting to examine why, beyond R_{HII} , $\alpha(R)$ remains high in some disks and drops sharply in others. Figure 9 shows the gas surface density profiles for the same ten galaxies. The HI disks of the Virgo cluster galaxies NGC 4394, NGC 4402, and NGC 4689 appear to have been stripped at radii $R \geq R_{\text{HII}}$. When the molecular gas density is included the difference in total gas surface density relative to the field galaxies is reduced, but the Virgo members still tend to have lower values of the instability parameter outside R_{HII} . Inspection of Figure 3 shows that the Virgo galaxies show HII regions beyond R_{HII} less frequently than the field sample.

3.5.3. Variations in the Threshold Stability Parameter with Galaxy Type

Figure 10 shows our best estimates of $\alpha(R_{\text{HII}})$ at the outer edges of 26 disks.³ The significance of the weak trend with galaxy type is difficult to assess quantitatively. The error bars represent limiting values and are set by the magnitude of systematic errors associated with one-dimensional gas profiles in non-axisymmetric disks, tidal disturbances, the extrapolation of the CO intensity profile to larger radii, and disk inclination. The dominant error terms differ in the early-type and late-type disks, so we discuss their $\alpha(R_{\text{HII}})$ values separately.

The earlier type disks (Sa to Sb) in Figure 10 tend to have $\alpha(R_{\text{HII}})$ values lower than the sample median. The discrepancy is not significant for NGC 2903, NGC 4321, and NGC 7731. The range of α values shown for each of them is consistent with the sample median, 0.69, because corrections for non-axisymmetric structures were shown to drive α in this direction (S 3.5.1). The $\alpha(R_{\text{HII}})$ values for the early-type galaxies NGC 4394, NGC 4402, NGC 4579, and NGC 4689 range from 0.5 to 0.6 and depend on extrapolations of the CO intensity profile. In all of the galaxies where molecular gas dominates the gas density at the threshold, α is less than or equal to 0.69; and most of these galaxies are type Sab-Sbc. It is unlikely that the gas surface density is systematically underestimated in these disks because the two largest biases in interpretation of the CO measurements work to increase the molecular gas density. First, since the CO emission is not well-resolved, particularly in NGC 4394, NGC 4402, and NGC 4689, the tendency is to overestimate scale lengths and artificially raise the molecular gas surface density at the threshold radii. Second, the CO/H₂ conversion factor is expected to be lower in disks with low metallicity.

³The six galaxies with sub-critical disks are omitted. NGC 5194 and NGC 5457 are not shown since the rotation curves are not well-defined at R_{HII} .

If the early-type spirals are more evolved than the late-type spirals, i.e. have consumed a larger fraction of their original gas content, then they should have higher metallicity on average. Hence, we have no reason to expect a low CO/H₂ conversion factor in the early-type galaxies. It is plausible then that the $\mu_{gas}/\mu_{crit}(R_{HII})$ ratios are somewhat lower than the mean in these early-type disks.

In contrast, the threshold values of the instability parameter for the HI-dominated edges scatter to both sides of 0.69. Lower mean metallicities in the later-type disks would introduce an artificial negative slope in Figure 10, which is not seen. We find no trend toward higher values of the instability parameter in late-type galaxies. In NGC 628, the estimated threshold value of the instability parameter, $\alpha(R_{HII}) = 0.86$, is consistent with the mean, $\alpha_Q = 0.69$, given the uncertainty in the rotation speed described in § 3.5.1. In NGC 925, the instability parameter is overestimated on the western side of the galaxy when the offset between the photometric and dynamical centers of this galaxy are neglected. (The kinematic radius is smaller than the H α radius, so κ is higher than we estimated assuming common photometric/dynamic centers.) A detailed analysis using $\sigma_g = 10 \text{ km s}^{-1}$ found α is 0.3 at the threshold (Pisano et al. 2000) which corresponds to $\alpha = 0.5$ for our assumed value of $\sigma = 6 \text{ km s}^{-1}$. Evaluation of the instability is particularly difficult in these late-type spirals, owing to the non-axisymmetric structures. We find no trend toward lower $\alpha(R_{HII})$ in the low angular velocity galaxies in our sample, all of type Scd to the Sdm, as one might have expected based on the low α values reported in dwarf irregular galaxies (HEB98).

3.5.4. Conclusions

The asymmetries of many disks in the sample compromise the accuracy of the stability analysis. We have demonstrated, however, that when disks are examined along position angle cuts that eliminate this uncertainty, the convergence of the stability profiles at the threshold radii is tighter. Outside the threshold radius, the disks with gas densities well below the critical density do not show many HII regions while those with prominent populations of HII regions tend to be near the threshold surface density. The weak trend toward lower values of α_Q in earlier type spiral galaxies is consistent with these disks having a larger stellar mass fraction (e.g. Jog & Solomon 1984).

3.6. Inner Disk Thresholds

We also examined whether simple gravitational stability arguments might be as successful describing star formation thresholds in the inner regions of disks as we have shown them to be at the outer edge of star forming disks.

The sharpest star formation thresholds in the inner disk are associated with rings of intense star formation activity – e.g. see NGC 4569, NGC 4579, NGC 4639, and NGC 4736 in Figure 3. Does the instability parameter, $\alpha(r)$, increase across these rings? The beamwidth of the HI and CO observations is inadequate to evaluate the instability parameter across the rings in NGC 4569 and NGC 4639. The major axis instability profile across NGC 4579 reaches $\alpha = 0.6$ on the western side of the ring, but the gas density along the eastern major axis is much lower than the critical density. The ring of HII regions in NGC 4579 is brighter on the west side than the east side, so star formation in the ring appears to be correlated with higher values of the instability parameter, i.e. lower Q values. In NGC 4736, the ring of HII regions at $R \sim 45''$ coincides with an inner Lindblad resonance (Gerin et al. 1991; Gu et al. 1996; Wong & Blitz 2000). The spatial resolution of the gas data does not resolve the 680 pc wide ring, but the lower limits on the gas surface density in the ring are sufficient to raise the instability parameter to values of 0.6 to 1.0. near the inner edge of the ring ($R \approx 34''$). Higher resolution data indicate $Q < 1$ in localized regions of the ring and $Q \sim 3$ averaged across the ring (Wong & Blitz 2000).

A few galaxies without rings have gas surface densities less than $0.69\mu_{crit}$ in their inner disks. We show the $\alpha(R)$ profiles for the three with the best spatial resolution in Figure 11. We expect to see little H α emission at radii less than the inner threshold radii in these galaxies. In Figure 3, the disks of NGC 628 and NGC 4535 show little star formation inside the predicted threshold radii of $70''$ and $50''$, respectively. Star formation in the central region of NGC 4178 is confined to the bar, where the gas density is likely higher than the azimuthal average, so the star-forming regions may not be sub-critical. The inner thresholds in these three galaxies are therefore consistent with the gravitational threshold model. Only the star formation in the central region of NGC 2403 is in direct conflict with the gravitational threshold model.

The inner regions of many spiral galaxies have a deficit of H α emission, relative to a fitted exponential disk – e.g. NGC 628, NGC 925, NGC 2403, NGC 3031, NGC 4321, NGC 4394, NGC 4535, and NGC 5236. Aside from the cases already discussed and NGC 4394, these breaks in the H α surface brightness profile are not large enough to be called star formation thresholds. This property of the H α surface brightness profiles was noticed by Hodge & Kennicutt (1983), but the physical cause has not been established. The region of low SFR is clearly associated with a bar in NGC 5236, NGC 4394, and

NGC 925. The inner threshold in NGC 3031 coincides with the inner Linblad resonance. Many galaxies with central H α deficits have sub-critical gas surface densities in the inner disk, and those with supercritical gas densities have bars or resonances. The only galaxy in this list with a supercritical gas density in the center and no identified bar or resonance is NGC 4321. Apparently, bars and resonances can inhibit star formation in the central regions of disks that are unstable to axisymmetric perturbations.

4. Discussion

Our results support previous studies which have claimed that the outer edges of spiral disks are well described by the gravitational stability of a single fluid, isothermal gas disk (Kennicutt 1989). We have shown that this criterion is often a good description of star formation thresholds in the inner disk as well. The aim of this section is to gain further insight into the underlying physical processes that regulate disk star formation. We examine the galaxies where the gravitational instability model fails and evaluate the utility of a qualitatively different threshold condition. A clear prediction of the gravitational threshold scenario is that the stellar disks should affect α_Q . We examine whether first-order accounting of the stellar disk changes the scatter in the distribution of α (R_{HII}) measurements. Finally, the impact of these star formation thresholds on the global star formation rate is summarized.

4.1. Shear Models

4.1.1. NGC 2403 and M 33

The gas density in the inner 240'' of NGC 2403 is below the critical value and less than half the critical density within 150'' of the center of the disk. Yet the inner half of the disk is covered with HII regions. No other galaxy in our sample presents widespread star formation in regions where the gas disk is predicted to be stable. This contradiction, and the very similar situation in M 33, were noticed by Kennicutt (1989). The most obvious explanations have been dismissed by Thornley & Wilson (1995). In particular, if the H₂/CO conversion factor were as much as five times higher than the Milky Way value, the implied increase in the molecular gas density would bring the total gas density up to the critical density in the inner disk without affecting the good agreement at the outer threshold. Comparison of virial and molecular masses for clouds in M 33, however, indicate the conversion factor is similar to the Galactic one (Wilson 1995). The metallicity and

rotation speed of M 33 are similar to NGC 2403, so Thornley & Wilson find no reason to suspect a higher surface density of molecular gas in either galaxy.

The star-forming disks in many dwarf irregular galaxies also appear to be sub-critical when the Toomre Q parameter is used to estimate the critical density, and it has been suggested that the shear criterion, Eqn. 5, describes the critical density better than the Toomre Q criterion (Hunter & Plummer 1996; HEB98). The disks of NGC 2403 and M 33 share an important dynamical property with dwarf irregular galaxies. The shear rate is low in the inner disk where the rotation speed is rising slowly with radius. The disk stability analysis for the irregulars, while quite interesting, is not yet compelling. Large systematic uncertainties arise from the highly irregular shape of the disks, greater uncertainty about the CO/H₂ conversion factor at very low metallicities, and the assumption that the molecular/atomic gas fraction is constant with radius.

Figure 12 compares the shear criterion for the critical density to the Toomre critical density across NGC 2403 and M 33. The gas surface densities for M33 data come from Newton (1980) and Young et al. (1995), and the threshold radius for star formation is 29'. In both spiral galaxies, the gas surface density exceeds μ_{crit}^A but falls below the Toomre critical density. The presence of widespread star formation can be interpreted as evidence that cloud formation is limited by the time available for cloud growth (in the presence of shear) rather than gravitational instability. It remains unclear whether this explanation is correct. One disk in our sample, e.g. NGC 4535, has an inner threshold which is well-described by the Q criterion but not the shear criterion. Also, models of self-regulated star formation predict $Q \sim 1$ throughout the disk (Silk 1997). Departure from this equilibrium condition may indicate the disk is in a transient state. The unusually high infall rate of neutral hydrogen onto the NGC 2403 disk, and perhaps M 33 as well, support this view (Schaap, Sancisi, & Swaters 2000; Sancisi et al. 2000).

4.1.2. Shear Criterion at the Outer Threshold

The galaxies in our sample generally have flat rotation curves at the threshold radius, so the critical density based on the Toomre Q criterion reduces to

$$\mu_{crit} = \alpha_Q \frac{1.41\sigma\Omega}{\pi G}. \quad (10)$$

The shear criterion for the critical density has the same radial dependence where the rotation speed is constant,

$$\mu_{critA} = \alpha_A \frac{0.5\sigma\Omega}{\pi G}. \quad (11)$$

Since the fitted value of $\alpha_Q = 0.69$, we need $\alpha_A = 2.0$ to obtain $\mu_{gas} = \mu_{critA}$ at R_{HII} for the disks with constant rotation speed at R_{HII} . This normalization factor is very close to that predicted by Elmegreen (Elmegreen 1993; Hunter, Elmegreen, & Baker 1998). If the rotation speed is constant at the outer threshold, then no distinction can be made between these two criteria for the outer edge of a disk.

The galaxies in our sample with the largest gradients in rotation speed at R_{HII} are NGC 4254, NGC 4394, NGC 4402, NGC 4535, and NGC 4569. The gradient in NGC 4394 is highly uncertain due to the low resolution of the HI position – velocity diagram for NGC 4394. Figure 13 compares the Toomre (top panel) and shear (bottom panel) representations of the critical density for the other four galaxies. The scatter among the values of μ_{gas} / μ_{crit} is actually smaller for the shear model than the Toomre Q model. However, when the α_A term in the shear criterion is normalized using the galaxies with flat rotation curves at R_{HII} , as represented by NGC 2403 and M 33 in Figure 13, the scatter in the $\mu_{gas} / \mu_{crit} (R_{HII})$ values exceeds that obtained with the Toomre Q criterion. The shear criterion does not appear to be as robust an indicator of the edges of star-forming disks in spiral galaxies as the Toomre criterion. The shear model was also unable to adequately describe the edges of the disks in dwarf irregular galaxies (Hunter et al. 1998).

4.2. The Influence of Stellar Disks on Instability

Real galaxies contain both gas and stars, and the system can be unstable even when both the stellar and gaseous components individually meet the requirements for stability (Jog & Solomon 1984; Elmegreen 1995; Wang & Silk 1994). Wang & Silk give an effective Q parameter for this two-fluid instability such that $Q_{eff} = \alpha_{eff}Q$, where

$$\alpha_{eff} = (1 + \mu_* \sigma_g / (\mu_g \sigma_*))^{-1}. \quad (12)$$

In the limit of a low stellar surface density or large stellar velocity dispersion, we have $\alpha_{eff} \approx 1.0$; and α_{eff} gets smaller as the stellar disk becomes more unstable relative to the gaseous disk. Following Wang & Silk, the parameters for the Milky Way disk yield $\alpha_{eff} = 0.72$ in the solar neighborhood.

How much should we expect this parameter to vary over our sample? The gas disk is a smaller fraction of the total gas mass in the earlier type galaxies, so the stellar disks are expected to have a more important influence on the stability of those disks. Scaling to the disk of the Milky Way (e.g. Kenney & Young 1989), the measured rotation velocities of these disks at R_{HII} imply average surface densities of 15 to 300 $M_\odot \text{ pc}^{-2}$. If the other parameters are held at their solar neighborhood values, then the highest surface density

disks should become unstable at a value of μ_{gas} / μ_{crit} that is $\sim 25\%$ lower than α_Q in the lower density disks. In other words, we would not be surprised to see α_Q values ranging from 0.25 to 1.0 across our sample. Better measurements of the stellar velocity dispersion and surface density would be needed to test whether the lack of such a trend poses a problem for the gravitational instability model.

4.3. Consequences for Star Formation Prescriptions

We have presented a picture where a single parameter, the gas surface density relative to the critical density for gravitational instability, determines whether the disk forms stars. Evolution in the cosmic star formation rate is likely driven, at least in part, by the evolution in the rate of galaxy – galaxy interactions with lookback time (e.g. Tan et al. 1999). In our star formation recipe, the environment influences the SFR indirectly through its impact on the large-scale gas distribution. Including the star formation threshold in the recipe allows the SFR to react non-linearly to small changes in the gas distribution.

Our H α atlas demonstrates that the distribution of star-forming regions in many disks is better described as *asymmetric* rather than *axisymmetric*. The correlations we find between local values of the instability parameter and the distribution of HII regions clearly indicate that the Toomre Q parameter provides useful guidance about the location of star forming regions in these disks. For example, in § 3.5.1, we found that disks are more unstable on the side with the higher star formation rate. Prior to that we showed that star formation at sub-critical radii in NGC 2903, NGC 3031, and NGC 4548 is confined to the spiral arms. The average gas surface density was within a factor of three of the critical value in all three cases. The increase in gas surface density in the arms is expected to be larger than the increase in the epicyclic frequency κ (and hence critical density) caused by unresolved, streaming motions (Rand 1993; Elmegreen 1994), so the arm gas may be supercritical locally. Since these features will not be resolved in cosmological simulations either, it would be reasonable to lower the α_Q value in Eqn. 2 from 0.69 to ~ 0.3 in galaxies undergoing weak interactions to account for unresolved, super-critical structure in the gas distribution

The fraction of gas residing in sub-critical regions of disks varies widely among the galaxies in our sample. Accounting for gas beyond the threshold radius produces the most significant correction to the global star formation rate. Among the spiral galaxies in our sample, the gas mass interior to the threshold radius R_{HII} varies from 0.14 to 0.94 of the total gas mass. Omitting the threshold radius from a model therefore leaves the global star formation rate uncertain by a factor of ~ 7 . The median value of the gas fraction interior

to R_{HII} is 0.6. Ram pressure stripping has removed diffuse, atomic gas from at least these Virgo cluster galaxies – e.g. NGC 4394, NGC 4402, NGC 4569, and NGC 4689 (Warmels 1988a, 1988b; Giovanelli & Haynes 1983; Kenney & Young 1989); yet a histogram of the gas mass fraction within R_{HII} for the Virgo subsample is indistinguishable from the histogram for the field subsample.

5. Summary

Using a larger sample of spiral galaxies than previous studies, we tested the thesis that widespread star formation occurs where the gas disk is unstable to axisymmetric perturbations. We located the edge of the star-forming disk using our new $\text{H}\alpha$ photometry, measured the gas surface density there, and derived the critical surface density for gravitational instability using the Toomre Q criterion. Our results confirm previous work by Kennicutt (1989) which found the threshold gas density varied by at least an order of magnitude among spiral galaxies but that the ratio of the gas density to the critical density was much more uniform. Among 26 galaxies with well-defined thresholds, we found the median ratio of gas surface density to critical density is $\alpha_Q = 0.69 \pm 0.2$, with $\alpha(R_{\text{HII}})$ defined by eq. (2) and an assumed gas velocity dispersion of 6 km s^{-1} . At the thresholds, the gas is primarily atomic (molecular) in the disks with the lowest (highest) gas surface density. These results confirm the surprising accuracy with which a simple stability criterion describes the extent of the star-forming disk in large, objectively-defined samples of galaxies.

This work also exposes the limitations of that simple model. The azimuthally-averaged, threshold values of the instability parameter, $\alpha(R_{\text{HII}})$, range from 0.3 to 1.2. A large part of that dispersion is due to uncertainties associated with asymmetric gas distributions, asymmetric mass distributions, and the extrapolation of the molecular gas surface density profiles. We demonstrated that the scatter in $\alpha(R_{\text{HII}})$ values is significantly reduced when R_{HII} and $\alpha(R_{\text{HII}})$ are fitted as functions of position angle. This result demonstrates that the simple Toomre Q stability criterion is useful for describing the distribution of star forming regions even in disks with quite non-axisymmetric gas distributions. The weak trend toward lower values of $\alpha(R_{\text{HII}})$ in Sab-Sbc galaxies, however, is not easily explained by any of the above systematics. These early-type spiral galaxies tend to have more massive stellar disks, so the lower values of α_Q would be consistent with the predicted de-stabilizing effect of a stellar disk on the gas disk. We find several sharp thresholds in the inner disks that are well described by gravitational stability alone. Star formation is also suppressed in the centers of a few disks where the gas density is super-critical, but each of these disks

has a strong stellar bar. More detailed analysis of the star formation rate in the inner region of disks requires higher spatial resolution (cf. Jogee 1999; Jogee et al. 2001). We conclude that streaming motions in the disk and the gravitational attracton of the stellar disk require small corrections to the simple instability parameter. Much of the uncertainty in current estimates of the instability parameter, however, should be resolved with complete two-dimensional mapping of the gas surface density and velocity field (e.g. Thornley et al. 1999).

One clear failure of the gravitational threshold model remains two sub-critical disks with widespread star formation in the inner disk – NGC 2403 and M 33. Both are low mass disks with low shear rates (i.e. slowly rising rotation curves). Elmegreen (1993) and HEB98 have suggested that star formation is limited by the time available for clouds to grow via inelastic collisions (in the destructive presence of disk shear) rather than cloud formation, which they argue happens easily via magnetic instabilities. We demonstrate that their shear criterion offers an explanation for the high star formation rates in the inner disks of NGC 2403 and M 33 but find it does not consistently predict the outer (or inner) threshold radii. The vertical structure of these disks is also unusual in that the infall rate is high, and the high star formation rates may be indirectly related to this transitional state. Since the star formation rate depends more naturally on gas volume density rather than surface density, the impact of the vertical structure of gas disks on the star formation law remains an important issue in a more general sense. Unfortunately, radial variation in the gas velocity dispersion remains controversial due to the difficulty of the measurement (e.g. Ferguson et al. 1998; Sellwood & Balbus 1999). Among the galaxies in our sample, the intrinsic dispersion in the threshold value of the instability parameter is small for a constant velocity dispersion leaving little motivation for strong variation in velocity dispersion with radius. Given the difficulties in measuring velocity dispersions accurately, the issue could be settled by comparing the threshold radii reported here to models of the transition radius from disk self-gravity to halo self-gravity.

The utility of the Toomre Q criterion extends beyond axisymmetric perturbations. Previous studies of sub-critical disks have focused on low surface brightness galaxies, which also have lower than average gas surface density. We showed that star-formation is similarly suppressed in disks with normal gas surface density if the rotation speed is fast enough to stabilize the disk. As the gas density approaches the critical density for instability, more isolated HII regions appear in the sub-critical disks. Similarly, in star-forming disks, HII regions are found outside the threshold radius most frequently when the gas density in the outer disk is near (i.e. within a factor of three roughly) the critical density. Star formation is sometimes confined to a spiral density wave in these sub-critical environments, and the co-rotation radius of the spiral pattern may describe the outer edge of the star-formation

activity. This result seems to support the view advanced by Rudnick, Rix, & Kennicutt (2000) that tidal interactions impart a significant boost to the star formation rate in disk galaxies.

Star formation thresholds in the outer disk change one’s view of disk star formation in two ways. First, in a typical disk today, roughly 40% of the gas mass is not included in the empirical relation that defines the global Schmidt law for the SFR, and the analogous correction should be made when global star formation laws are applied in simulations. Second, disks are clearly not perfectly self-regulated if their outer disks are not forming stars. Significant velocity dispersions in these regions imply a physical process other than feedback from massive stars contributes to disk heating (Sellwood & Balbus 1999). Because of the threshold effect in the star formation law, the central density and angular momentum of the halo are clearly of fundamental importance to the star formation history of a disk galaxy (Dalcanton, Spergel, & Summers 1997; Mo et al. 1998; Mao et al. 1998)

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Table 1: Data

Galaxy	Type ^d	d(Mpc)	ι^e	PA(°)	H α ^a	Reference (d, RC, HI, CO)
NGC 628	SA(s)c	11.4 ^b	5°	25	K36	1, 2 and 3, 1
NGC 925	SAB(rs)cd	9.3	55.2°	102	S90	4, 2 and 5, 2, 1
NGC 2403	SAB(s)cd	3.6	60°	125	BS	6, 2 and 5, 2, 1
NGC 2841	SA(r)b	10.0 ^b	68°	148	K36	1, 7, 7, 1
NGC 2903	SAB(rs)bc	6.6 ^b	60.0°	44	S90	1, 2, 2, 1
NGC 3031	SA(s)ab	3.6	58.7°	149	BS	8, 9, 10, 11
NGC 4178	Sdm	17.0	69.0°	30	S90	12, 13, 14, 15
NGC 4254	SA(s)c	17.0	28°	56	S90	12, 13, 14, 15
NGC 4321	SAB(s)bc	16.1	30°	120	S90	16, 17, 14, 15
NGC 4394	(R)SB(r)b	17.0	25°	108	S90	12, 18, 14, 15
NGC 4402	Sb	17.0	75.0°	90	S90	12, 13, 14, 15
NGC 4501	SA(rs)b	17.0	58.0°	140	K36	12, 13, 14, 15
NGC 4535	SAB(s)c	16.3	44°	0	S90	19, 13, 14, 15
NGC 4548	SBb(sr)	16.1	33°	136	S90	6, 37, 14, 15
NGC 4569	SAB(rs)ab	17.0	65°	19	S90	12, 13, 14, 15
NGC 4571	SA(r)cd	17.0	28°	55	S90	12, 20, 14, 15
NGC 4579	SAB(rs)b	17.0	36°	95	S90	12, 13, 14, 15
NGC 4639	Sbc	17.0	45°	123	S90	12, 37, 14, 15
NGC 4647	SAB(rs)c	17.0	37°	110	S90	12, 20, 14, 15
NGC 4651	SA(rs)c	17.0	42°	71	S90	12, 18, 14, 15
NGC 4654	SAB(rs)cd	17.0	52°	128	S90	12, 13, 14, 15
NGC 4689	SA(rs)bc	17.0	30°	165	S90	12, 13, 14, 15
NGC 4698	SA(s)ab	17.0	57°	164	S90	12, 18, 14, 15
NGC 4713	SAB(rs)d	17.0	49.0°	100	K36	12, 20, 14, 15
NGC 4736	(R)SA(r)ab	4.7 ^b	35°	122	K36	1, 21, 21, 1
NGC 4826	(R)SA(rs)ab	5.4 ^b	52°	112	S90	1, 22, 22, 1
NGC 5055	SA(rs)bc	8.4	55.2°	99	K36	1, 2, 2, 1
NGC 5194	SA(s)bc pec	8.1	20°	170	BS	1, 23, 24, 25
NGC 5236	SAB(s)c	4.1 ^c	23.9°	225	BS	26, 27, 27, 1 (36)
NGC 5457	SAB(rs)cd	7.4	18°	44	BS	28, 29 and 30, 30, 29
NGC 6946	SAB(rs)cd	4.8	30.0°	62	BS	21, 32, 33, 34
NGC 7331	SA(s)bc	15.1	74.9°	167	S90	35, 7, 7, 1

^aNote. – Telescope used for H α observation: Burrell-Schmidt (BS); KPNO 36-in (K36); Steward 90-in (S90).

^bPublished distance adjusted to $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

^cDistance to M83 group.

^ddeVaucouleurs type from RC1

^eInclination of the disk such that a face-on orientation is 0 degrees.

References. — (1) Young et al. 1995; (2) Wevers et al. 1986; (3) Kamphuis & Briggs 1992; (4) Silbermann et al. 1996; (5) Pisano, Wilcots, & Elmegreen 1998; (6) Graham et al. 1998; (7) Bosma 1981; (8) Freedman et al. 1994b; (9) Adler & Westpfahl 1996; (10) Rots 1975; (11) Sage & Westpfahl 1991; (12) Freedman et al. 1994a; (13) Guhathakurta et al. 1988; (14) Warmels 1988c; (15) Kenney & Young 1988; (16) Ferrarese, L. et al. 1996, ApJ, 464, 568. (17) Sofue 1997; (18) Warmels 1988a; (19) Macri et al. 1998; (20) Warmels 1988b; (21) Bosma 1977; (22) Braun et al. 1994; (23) Sofue 1996; (24) Tilanus & Allen 1991; (25) Lord & Young 1990; (26) Saha et al. 1995; (27) Tilanus & Allen 1993; (28) Kelson et al. 1996; (29) Kenney et al. 1991; (30) Bosma, Goss, & Allen 1981; (31) Sharina et al. 1997; (32) Carignan et al. 1990; (33) Tacconi & Young 1986; (34) Tacconi & Young 1989; (35) Hughes et al. 1998; (36) Crosthwaite et al. 2000 (in prep); (37) Rubin et al. 1999.

FIGURE CAPTIONS

Fig. 1.— Integrated $H\alpha + [NII]$ fluxes vs published values of Kennicutt & Kent (1983) and Kennicutt (1998). Open symbols denote galaxies with dependent calibrations – i.e. the data presented here were calibrated using the data plotted along the abscissa.

Fig. 2.— (top) The $H\alpha$ surface brightness profile for NGC 5236. The dashed line is the fitted exponential disk. The threshold radius is shown by the dotted line. (middle) Radial variation in gas surface density. Filled/open circles represent molecular gas density along the major axis from Young et al. (1995) and Crosthwaite & Turner (private communication). The squares show the azimuthally-averaged atomic hydrogen surface density (Tilanus & Allen 1993). (The H densities were multiplied by a factor of 1.4 to include the He mass.) The inner and outer spiral arms imprint the local HI maxima at $120''$ and $240''$. The dashed line is the critical surface density for local gravitational instability. (bottom) Ratio of total gas surface density to critical density.

Fig. 3.— Atlas of $H\alpha + [NII]$ images and radial surface brightness profiles. A vertical, dotted line marks the radius of the threshold in the azimuthally-averaged star formation activity. Dashed lines show variations in threshold radius with position angle. North and east are marked with bars $30''$ long.

Fig. 4.— Radial variation of the instability parameter in sub-critical disks. If no threshold radius was found, the radius of maximum instability was used to normalize the abscissa.

Fig. 5.— Gas surface density in sub-critical disks.

Fig. 6.— Mass fraction of atomic gas versus total gas mass at the star formation thresholds. The sub-critical disks are represented by open triangles.

Fig. 7.— Azimuthal variation in the instability parameter. The solid lines represent an azimuthal average. The dashed lines are cuts along the major axis. Note that in (b) the HI surface density was measured at position angles of $\pm 90^\circ$, and the molecular gas was measured along the major axis which is 60° off this HI strip.

Fig. 8.— Radial variation in the instability parameter. The disks with the least azimuthal variation in threshold radius are shown. The galactocentric radius is normalized to the threshold radius. Dotted lines mark the mean ratio of the gas surface density to the critical density at the threshold radius.

Fig. 9.— Radial variation in gas surface density. The disks with the least azimuthal variation in threshold radius are shown.

Fig. 10.— Instability parameter at the star formation threshold vs. revised morphological type (RC2 T-type) of the galaxy. (Note that galaxy type is an integer quantity, and the decimals are used merely to separate points.) Filled (open) symbols represent surface densities dominated by atomic (molecular) gas, respectively. From left to right, the points represent these galaxies: NGC 4736 (2.0), NGC 4826 (2.1), NGC 4569 (2.3), NGC 4394 (3.0), NGC 4402 (3.1), NGC 4501 (3.3), NGC 7331 (3.4), NGC 4579 (3.5), NGC 4689 (4.0), NGC 2903 (4.2), NGC 5055 (4.3), NGC 4321 (4.4), NGC 4651 (5.0), NGC 5236 (5.1), NGC 628 (5.2), NGC 4254 (5.3), NGC 4535 (5.4), NGC 4647 (5.5), NGC 2403 (6.0), NGC 6946 (6.1), NGC 4654 (6.3), NGC 925 (7.0), NGC 4713 (7.2), and NGC 4178 (8.0).

Fig. 11.— Instability parameter normalized to the location of the threshold in the inner disk. The dotted lines shown the median value of the instability parameter at the outer thresholds for reference.

Fig. 12.— Comparison of the Toomre Q and shear stability criteria in the inner disk. The observed gas surface density is shown by the solid line for comparison. The radial coordinate is normalized to the star formation threshold.

Fig. 13.— Comparison of the Toomre and shear instability parameters at the outer thresholds. The text describes why these six galaxies are shown.